

1. Calcule os seguintes limites:

$$(a) \lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x - 2}.$$

$$(b) \lim_{x \rightarrow \infty} \frac{2x^3 + 5x - 1}{x^3 - 4x^2 + 6}.$$

$$(c) \lim_{x \rightarrow -\infty} \frac{3x^4 + x^2 - 7}{5x^4 + 2x + 1}.$$

$$(d) \lim_{x \rightarrow -\infty} \frac{4x^7 - 3x + 2}{12x^8 + 7x^7 + 9x^4}.$$

$$(e) \lim_{x \rightarrow -\infty} \frac{3x^4 + x^2 - 7}{5x^4 + 2x + 1}.$$

$$(f) \lim_{x \rightarrow -7} \frac{x^2 - 49}{x + 7}.$$

$$(g) \lim_{x \rightarrow 0} \frac{x^3 + x^2}{x^2 + x}.$$

$$(h) \lim_{x \rightarrow \infty} \frac{7x^5 - x^3 + 1}{3x^5 + 2x^4 - x}.$$

$$(i) \lim_{x \rightarrow 2} \frac{2x^3 - 16}{x - 2}.$$

2. Determine:

$$(a) \lim_{h \rightarrow 0} \frac{\sqrt{9+h} - 3}{h}.$$

$$(b) \lim_{x \rightarrow \infty} \frac{\sqrt[3]{x^2+x} - x^{2/3}}{x^{1/3}}.$$

$$(c) \lim_{x \rightarrow \infty} \frac{\sqrt{x^2+2x} - x}{x}.$$

$$(d) \lim_{x \rightarrow 0} \frac{\sqrt{x^2+16} - 4}{x^2}.$$

$$(e) \lim_{x \rightarrow 0} \frac{\sqrt[3]{8+x} - 2}{x}.$$

3. Encontre:

$$(a) \lim_{x \rightarrow 0} \frac{\tan(x)}{x}.$$

$$(b) \lim_{x \rightarrow \pi/4} \frac{\sin(x) - \cos(x)}{\tan(x) - 1}.$$

$$(c) \lim_{x \rightarrow 0} \sin\left(\frac{1}{x}\right).$$

$$(d) \lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x^2}.$$

$$(e) \lim_{x \rightarrow 0} \frac{\sqrt{1 - \cos^2(x/2)}}{x}.$$

$$(f) \lim_{x \rightarrow 0} x \csc(x).$$

4. Determine

$$\lim_{x \rightarrow a^-} f(x), \quad \lim_{x \rightarrow a^+} f(x), \quad \text{e } \lim_{x \rightarrow a} f(x)$$

para cada uma das seguintes funções e valores de a :

$$(a) a = 1,$$

$$(b) a = 0,$$

$$(c) a = -1,$$

$$f(x) = \begin{cases} x^2 & \text{se } x < 1, \\ 2x - 1 & \text{se } x \geq 1. \end{cases} \quad f(x) = \begin{cases} 2x + 3 & \text{se } x < 0, \\ x^2 - 1 & \text{se } x \geq 0. \end{cases} \quad f(x) = \begin{cases} (x+1)^2 & \text{se } x \leq -1, \\ x^2 + 1 & \text{se } x > -1. \end{cases}$$

5. Calcule os seguintes limites:

$$(a) \lim_{x \rightarrow 0} \frac{1}{x} \left(1 - \frac{1}{(x+1)^3} \right)$$

$$(b) \lim_{x \rightarrow -7} \frac{1}{x+7} \left(\frac{1}{x} + \frac{1}{7} \right).$$

$$(c) \lim_{x \rightarrow 0} \frac{1}{x} \left(1 - \frac{1}{(x+2)^2} \right).$$

$$(d) \lim_{x \rightarrow 1} \frac{1}{x-1} \left(\frac{1}{x^2} - 1 \right).$$

$$(e) \lim_{x \rightarrow 0} \frac{1}{x^3} ((x+1)^4 - 1).$$

$$(f) \lim_{x \rightarrow 0} \frac{1}{x} \left(\frac{1}{(x+1)^2} - \frac{1}{(x+2)^2} \right).$$